## Finding the Equation of a Polynomial Function

In this section we will work backwards with the roots of polynomial equations or zeros of polynomial functions. As we did with quadratics, so we will do with polynomials greater than second degree. Given the roots of an equation, work backwards to find the polynomial equation or function from whence they came. Recall the following example.

Find the equation of a parabola that has $\boldsymbol{x}$ intercepts of $(-3,0)$ and $(2,0)$. $(-3,0)$ and $(2,0) . \quad$ Given $x$ intercepts of -3 and 2

$$
\begin{array}{ll}
x=-3 & x=2
\end{array} \begin{aligned}
& \text { If the } x \text { intercepts are }-3 \text { and } 2 \text {, then the roots of the equation are }-3 \text { and } 2 \text {. Set each } \\
& \text { root equal to zero. }
\end{aligned}
$$

The exercises in this section will result in polynomials greater than second degree. Be aware, you may not be given all roots with which to work.

## Consider the following example:

Find a polynomial function that has zeros of 0,3 and $2+3$. Although only three zeros are given here, there are actually four. Since complex numbers always come in conjugate pairs, 2-3i must also be a zero. Using the fundamental theorem of algebra, it can be determined that his is a $4^{\text {th }}$ degree polynomial function.

Take the zeros of $0,3,2 \pm 3 i$, and work backwards to find the original function.

$$
\begin{array}{ccr}
x=0 & x=3 & x=2 \pm 3 i \\
& & x=2 \pm 3 i \\
& x=3 & x-2= \pm 3 i \\
x=0 & -3-3 & x^{2}-4 x+4=9 i^{2} \\
& x-3=0 & x^{2}-4 x+4=-9 \\
& & x^{2}-4 x+13=0 \\
x & (x-3) & \left(x^{2}-4 x+13\right)
\end{array}
$$

The polynomial function with zeros of $0,3,2 \pm 3 i$, is equal to $f_{(x)}=x(x-3)\left(x^{2}-4 x+13\right)$. Multiplying this out will yield the following.

$$
f_{(x)}=x^{4}-7 x^{3}+25 x^{2}-39 x
$$

